

## 9.2 Quadratic Inequalities in One Variable, pages 476–487

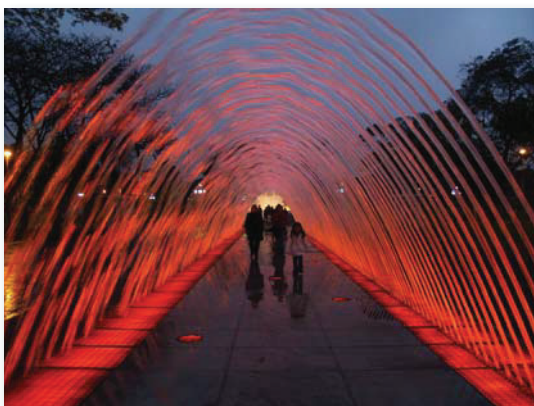
6. Choose a strategy to solve each inequality. Explain your strategy and why you chose it.

a)  $x^2 - 2x - 63 > 0$   
 b)  $2x^2 - 7x - 30 \geq 0$   
 c)  $x^2 + 8x - 48 < 0$   
 d)  $x^2 - 6x + 4 \geq 0$

7. Solve each inequality.

a)  $x(6x + 5) \leq 4$   
 b)  $4x^2 < 10x - 1$   
 c)  $x^2 \leq 4(x + 8)$   
 d)  $5x^2 \geq 4 - 12x$

8. A decorative fountain shoots water in a parabolic path over a pathway. To determine the location of the pathway, the designer must solve the inequality  $-\frac{3}{4}x^2 + 3x \leq 2$ , where  $x$  is the horizontal distance from the water source, in metres.



- a) Solve the inequality.  
 b) Interpret the solution to the inequality for the fountain designer.
9. A rectangular storage shed is to be built so that its length is twice its width. If the maximum area of the floor of the shed is  $18 \text{ m}^2$ , what are the possible dimensions of the shed?

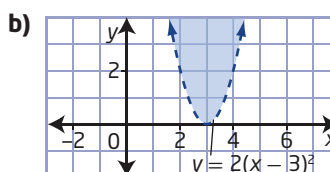
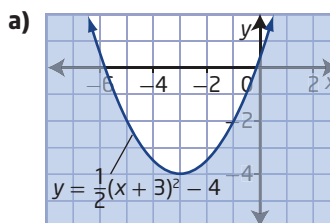
10. David has learned that the light from the headlights reaches about 100 m ahead of the car he is driving. If  $v$  represents David's speed, in kilometres per hour, then the inequality  $0.007v^2 + 0.22v \leq 100$  gives the speeds at which David can stop his vehicle in 100 m or less.



- a) What is the maximum speed at which David can travel and safely stop his vehicle in the 100-m distance?  
 b) Modify the inequality so that it gives the speeds at which a vehicle can stop in 50 m or less.  
 c) Solve the inequality you wrote in part b). Explain why your answer is not half the value of your answer for part a).

## 9.3 Quadratic Inequalities in Two Variables, pages 488–500

11. Write an inequality to describe each graph, given the function defining the boundary parabola.

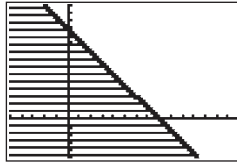


e)  $y \geq \frac{1}{12}x$



4. a)  $15x + 10y \leq 120$ , where  $x$  represents the number of movies and  $y$  represents the number of meals.

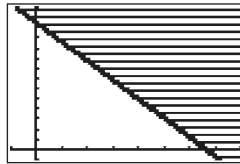
b)  $y \leq -1.5x + 12$



- c) The region below the line in quadrant I ( $x \geq 0, y \geq 0$ ) shows which combinations will work for her budget. The values of  $x$  and  $y$  must be whole numbers.
5. a) \$30 for a laptop and \$16 for a DVD player  
b)  $30x + 16y \geq 1000$ , where  $x$  represents the number of laptops sold and  $y$  represents the number DVD player sold.

c)  $y \geq -1.875x + 62.5$

- The region above the line in quadrant I shows which combinations will give the desired commission. The values of  $x$  and  $y$  must be whole numbers.



6. a)  $\{x \mid x < -7 \text{ or } x > 9, x \in \mathbb{R}\}$   
b)  $\{x \mid x \leq -2.5 \text{ or } x \geq 6, x \in \mathbb{R}\}$   
c)  $\{x \mid -12 < x < 4, x \in \mathbb{R}\}$   
d)  $\{x \mid x \leq 3 - \sqrt{5} \text{ or } x \geq 3 + \sqrt{5}, x \in \mathbb{R}\}$

7. a)  $\left\{x \mid -\frac{4}{3} \leq x \leq \frac{1}{2}, x \in \mathbb{R}\right\}$   
b)  $\left\{x \mid \frac{5 - \sqrt{21}}{4} < x < \frac{5 + \sqrt{21}}{4}, x \in \mathbb{R}\right\}$

c)  $\{x \mid -4 \leq x \leq 8, x \in \mathbb{R}\}$

d)  $\left\{x \mid x \leq \frac{-6 - 2\sqrt{14}}{5}\right.$   
or  $\left. x \geq \frac{-6 + 2\sqrt{14}}{5}, x \in \mathbb{R}\right\}$

8. a)  $\left\{x \mid \frac{6 - 2\sqrt{3}}{3} \leq x \leq \frac{6 + 2\sqrt{3}}{3}, x \in \mathbb{R}\right\}$

- b) The path has to be between those two points to allow people up to 2 m in height to walk under the water.

9. The length can be anything up to and including 6 m. The width is just half the length, so it is a maximum of 3 m.

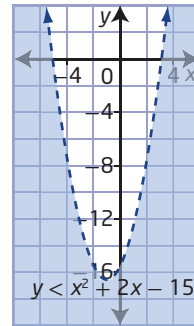
10. a) 104.84 km/h

b)  $0.007v^2 + 0.22v \leq 50$

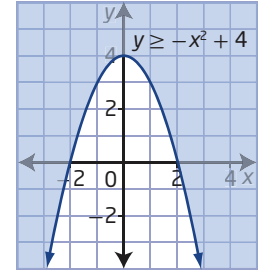
- c) The solution to the inequality within the given context is  $0 < v \leq 70.25$ . The maximum stopping speed of 70.25 km/h is not half of the answer from part a) because the function is quadratic not linear.

11. a)  $y \leq \frac{1}{2}(x + 3)^2 - 4$     b)  $y > 2(x - 3)^2$

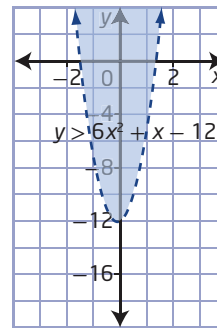
12. a)



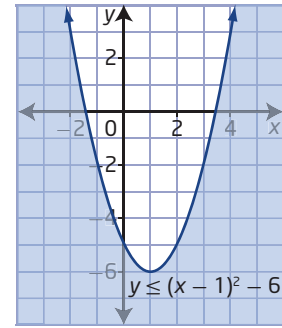
b)



c)



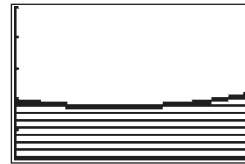
d)



13. a)  $y < x^2 + 3$

b)  $y \leq -(x + 4)^2 + 2$

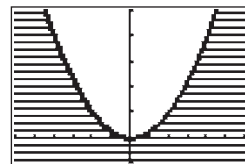
14. a)  $y \leq 0.003t^2 - 0.052t + 1.986,$   
 $0 \leq t \leq 20, y \geq 0$



- b)  $0.003t^2 - 0.052t - 0.014 \leq 0$ ; the years it was at most 2 t/ha were from 1975 to 1992.

15. a)  $r \leq 0.1v^2$

- You cannot have a negative value for the speed or the radius. Therefore, the domain is  $\{v \mid v \geq 0, v \in \mathbb{R}\}$  and the range is  $\{r \mid r \geq 0, r \in \mathbb{R}\}$ .



- b) Any speed above 12.65 m/s will complete the loop.

16. a)  $20 \leq \frac{1}{20}x^2 - 4x + 90$

- b)  $\{x \mid 0 \leq x \leq 25.86 \text{ or } 54.14 \leq x \leq 90, x \in \mathbb{R}\}$ ; the solution shows where the cable is at least 20 m high.